



Geometric Science of Information

SEE Conference

GSI'21 in Paris

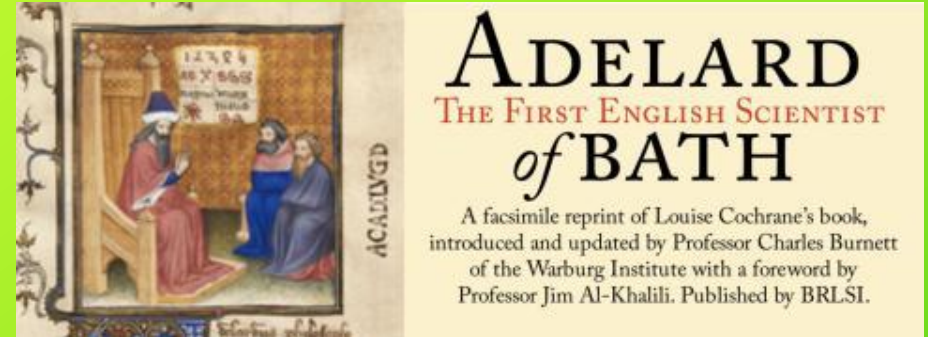
GSI General Chairmen: Frédéric BARBARESCO*, Frank NIELSEN**

(*) President of SEE ISIC Club (Ingénierie des Systèmes d'Information de Communications) & THALES Land & Air Systems, (**) Ecole Polytechnique/LIX & LIX & Sony CSL Tokyo

GSI Logo: Adelard of Bath



The frontispiece of an Adelard of Bath Latin translation of Euclid's Elements, c. 1309–1316; the oldest surviving Latin translation of the Elements is a 12th-century translation by Adelard from an Arabic version



- He left England toward the end of the 11th century for **Tours** in France
- Adelard taught for a time at **Laon**, leaving Laon for travel no later than 1109.
- After Laon, he travelled to **Southern Italy** and **Sicily** no later than 1116.
- Adelard also travelled extensively throughout the "lands of the Crusades": **Greece, West Asia, Sicily, Spain,** and potentially **Palestine.**

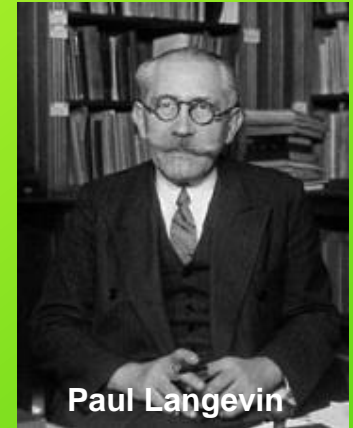
Adelard of Bath was the first to translate **Euclid's Elements in Latin**

Adelard of Bath has introduced the word « **Algorismus** » in Latin after his translation of Al Khuwarizmi

SEE at a glance



- Meeting place for science, industry and society
- An officially recognised non-profit organisation
- About 2000 members and 5000 individuals involved
- Large participation from industry (~50%)
- 19 «Clubs techniques» and 12 «Groupes régionaux»
- Organizes conferences and seminars
- Initiates/attracts International Conferences in France
- Institutional French member of IFAC and IFIP
- Awards (Glavieux/Brillouin Prize, Général Ferrié Prize, Néel Prize, Jerphagnon Prize, Blanc-Lapierre Prize, Thévenin Prize), grades and medals (Blondel, Ampère)
- Publishes 3 periodical publications (REE, ...) & 3 monographs each year
- Web: <http://www.see.asso.fr> and LinkedIn SEE group
- SEE Presidents: Louis de Broglie, Paul Langevin, ...



Paul Langevin



Louis de Broglie

1883-2019: From SIE & SFE to SEE: 136 years of Sciences

Société de l'électricité, de l'électronique et des technologies de l'information et de la communication



1881

Exposition Internationale d'Electricité



**1883: SIE
Société
Internationale
des Electriciens**

**1886: SFE
Société
Française
des Electriciens**



2013: SEE

**17 rue de l'Amiral Hamelin
75783 Paris Cedex 16**



GSI conferences ancestors

Séminaire Léon Brillouin

Sciences géométriques de l'information

2009-2014

<http://repmus.ircam.fr/brillouin/home>

<http://repmus.ircam.fr/brillouin/past-events>

**Leon Brillouin
Seminar
on
Geometric
Science of
Information
(Hosted by IRCAM,
Stravinsky Room)**

Videos & slides
available online

SÉMINAIRE LÉON BRILLOUIN

SCIENCES GÉOMÉTRIQUES
DE L'INFORMATION

Marc Arnaudon (IMB, Bordeaux)

Un algorithme stochastique pour trouver
les moyennes généralisées
sur les variétés compactes.

14 février 2014
IRCAM - Salle Stravinsky

ÉCOLE
POLYTECHNIQUE

THALES

ircam
Centre
Pompidou



GSI conferences ancestors

INDO-FRENCH

MIG'11 Matrix Information Geometry Workshop

(Ecole Polytechnique &
Thales Research & Technology, 2011)

Frank Nielsen · Rajendra Bhatia *Editors*

Matrix Information Geometry



Sponsored by le Centre
Franco-Indien pour la Recherche
de la Recherche Scientifique

CEFIPRA | IFCPAR

Sponsored by Indo-French
Centre for the Geometry of
Information Geometries

Indo-French Seminar

THALES

Matrix Information Geometries

Information Geometry

Structured Matrix Geometry

23-02/11-Thales Research & Technology (Auditorium) &
24-25/02/11 Ecole Polytechnique (Becquerel Lecture Hall), Saclay Campus - Palaiseau, France
website : <http://www.informationgeometry.org/MIG/>

<https://www.lix.polytechnique.fr/~nielsen/MIG/>

<https://www.lix.polytechnique.fr/~nielsen/MIG/FLYERS-MIG-Final-V2.pdf>

<https://www.lix.polytechnique.fr/~nielsen/MIG/MIG-proceedings.pdf>

THALES





GSI'13 Mines ParisTech

Slides :

<https://www.see.asso.fr/gsi2013>



GSI'15 Ecole Polytechnique

Videos:

<https://www.youtube.com/channel/UC5HHo1jbQXusNQzU1iekaGA>

UNITWIN website (slides & videos):

<http://forum.cs-dc.org/category/90/gsi2015>



GSI'17 Mines ParisTech

Videos: <https://www.youtube.com/channel/UCnE9-LbfFRqtaes49cN2DVg/videos>

UNITWIN website (slides & videos):

<http://forum.cs-dc.org/category/135/gsi2017>



GSI'19 ENAC in Toulouse



website :
<https://www.see.asso.fr/en/GSI2019>

Hirohiko Shima
Jean-Louis Koszul



Roger Balian



GSI'13 Mines ParisTech



GSI'15 Polytechnique



Charles-Michel
Marle

GSI'17 Mines ParisTech



Jean-Michel Bismut &
Yann Ollivier



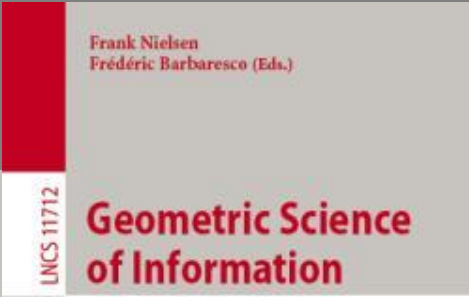
GSI SPRINGER PROCEEDINGS Collection

GSI'19 Springer Proceedings:
<https://www.springer.com/gp/book/9783030269791>

GSI'17 Springer Proceedings:
<http://www.springer.com/cn/book/9783319684444>

GSI'15 Springer Proceedings:
<http://www.springer.com/la/book/9783319250397>

GSI'13 Springer Proceedings:
<http://www.springer.com/us/book/9783642400193>

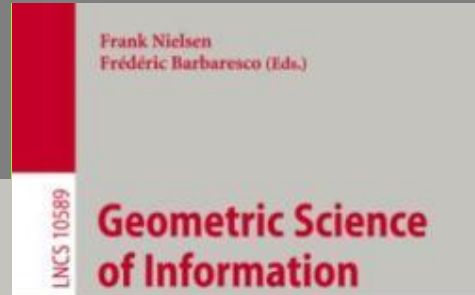


Frank Nielsen
Frédéric Barbaresco (Eds.)

LNCS 11712

Geometric Science of Information

4th International Conference, GSI 2019
Toulouse, France, August 27-29, 2019
Proceedings

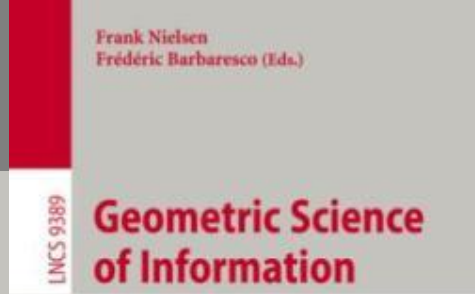


Frank Nielsen
Frédéric Barbaresco (Eds.)

LNCS 10589

Geometric Science of Information

Third International Conference, GSI 2017
Paris, France, November 7-9, 2017
Proceedings

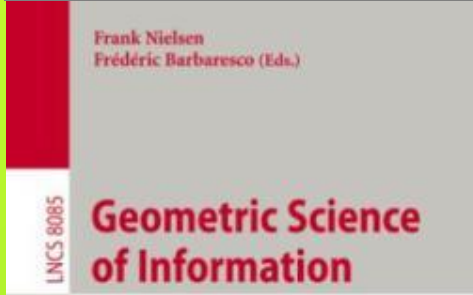
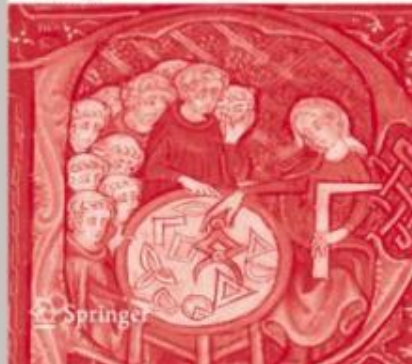


Frank Nielsen
Frédéric Barbaresco (Eds.)

LNCS 9389

Geometric Science of Information

Second International Conference, GSI 2015
Palaiseau, France, October 28-30, 2015
Proceedings

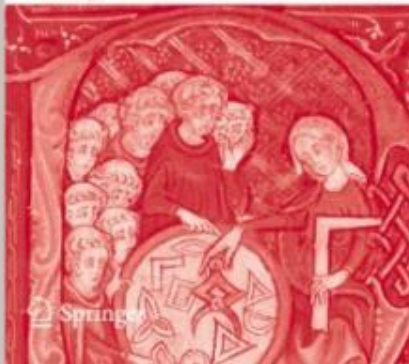


Frank Nielsen
Frédéric Barbaresco (Eds.)

LNCS 8085

Geometric Science of Information

First International Conference, GSI 2013
Paris, France, August 2013
Proceedings



Free SPRINGER GSI'19 Proceedings:
<https://link.springer.com/book/10.1007/978-3-030-26980-7>

CIRM Seminar, August 2017

TGSI'17 « Topological & Geometrical Structures of Information »



TGSI'17 videos & slides

<http://forum.cs-dc.org/category/94/tgsi2017>

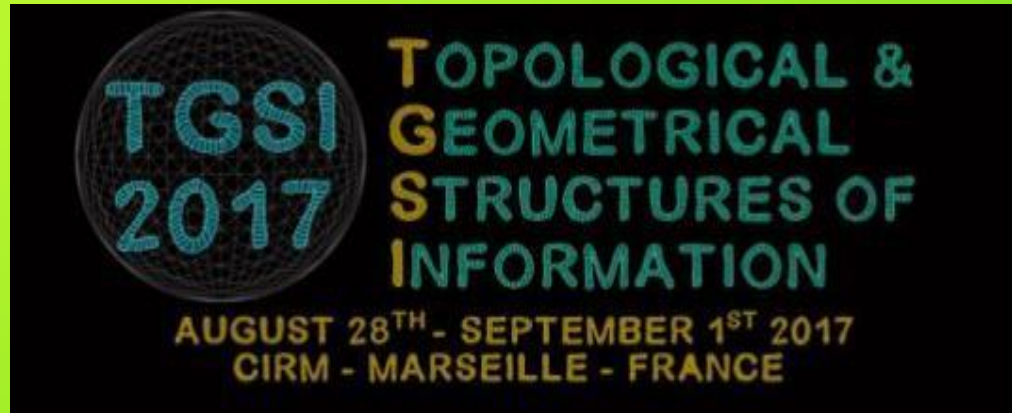
Special Issue "Topological and Geometrical Structure of Information", Selected Papers from CIRM conferences 2017"

http://www.mdpi.com/journal/entropy/special_issues/topological_geometrical_info



entropy

an open access journal by 



Talk on Koszul-Souriau Characteristic Function:

<https://www.youtube.com/watch?v=VXxiMCn-tsE&feature=youtu.be>



entropy
2018

From Physics to Information Sciences and Geometry

14-16 May 2018, Barcelona, Spain

$$H(S) = -\sum p_i \log_2 p_i$$

$$D_{KL}(p|m) = \int \log(f(x)/p(x)) p(x) dx = \int f(x) \log(f(x)/m(x)) dx$$

$$S = -k_B \sum p_i \ln p_i$$

$$S = -k_B \text{Tr}(\rho \ln \rho)$$

$$H = \int_{-\infty}^{\infty} f(x) \log(f(x) \Delta) dx$$

$$H(X, Y) = H(X|Y) + H(Y) = H(Y|X) + H(X)$$



14–16 May 2018

<https://sciforum.net/conference/Entropy2018-1>

From Physics to Information Sciences and Geometry

Barcelona, Spain

The main topics and sessions of the conference cover:

- Physics: classical Thermodynamics and Quantum
- Statistical physics and Bayesian computation
- Geometrical science of information, topology and metrics
- Maximum entropy principle and inference
- Kullback and Bayes or information theory and Bayesian inference
- Entropy in action (applications)

The inter-disciplinary nature of contributions from both theoretical and applied perspectives are very welcome, including papers addressing conceptual and methodological developments, as well as new applications of entropy and information theory.



Foundations of Geometric Structures of Information

4-6 Feb 2019 Montpellier (France)

Login

MAIN MENU

- Home
- Speakers
- Planning
- Registration
- List of Participants
- Documents of the conference
- Practical information
- Sponsors
- HELP

PRESENTATION

A seminar on Topological and Geometrical Structures of Information has been organized at CIRM in 2017, to gather engineers, applied and pure mathematicians interested in the geometry of information. This year FGSI'19 conference will be focused on the foundations of geometric structures of information. It is dedicated to the triumvirat Cartan - Koszul - Souriau and their influence on the field.

Poster



<https://fgsi2019.sciencesconf.org/>

FGSI'19 Cartan-Koszul-Souriau

Foundations of Geometric Structures of Information



Anton ALEKSEEV (Geneva Univ.)

Patrick IGLESIAS-ZEMMOUR (Aix-Marseille Univ.)

Dmitri ALEKSEEVSKY (Moscow IITP)

Yann OLLIVIER (Paris Facebook)

John BAEZ (Riverside UC)

Vasily PESTUN (Paris IHES)

Michel BRION (Grenoble Univ.)

Aissa WADE (Penn State Univ.)

Misha GROMOV (Paris IHES)

Panel sessions: SYMPLECTIC GEOMETRY IN PHYSICS

TRIBUTE TO J-L KOSZUL & J-M SOURIAU

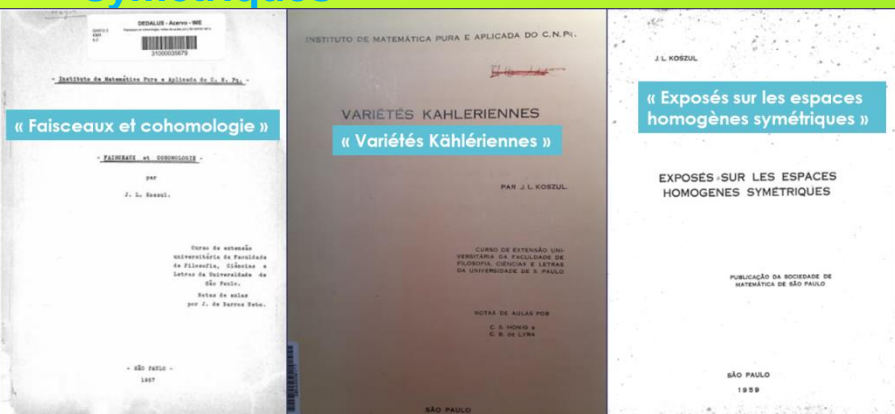




Jean-Louis Koszul was
foreign member of São Paulo
Academia of Sciences

Jean Louis Koszul Lectures
at Sao Paulo:

- **Faisceaux et Cohomologie**
- **Variétés Kählériennes**
- **Exposés sur les espaces homogènes symétriques**



Sao Paulo Journal of
Mathematical Sciences
SPRINGER
Editor-in-Chief: **Claudio
Gorodski**

<https://www.springer.com/mathematics/journal/40863>

2nd Workshop São Paulo Journal of Mathematical Sciences



**Jean-Louis Koszul in São Paulo
His Work and Legacy**

13-14 November 2019

Audithorium Antônio Gilioli, Institute of Mathematics and Statistics
University of São Paulo

Speakers:

Dmitri Alekseevsky (IITP Moscow)*
Michel Nguiffo Boyom (Montpellier)
Ugo Bruzzo (SISSA/UFPB)
Rui Loja Fernandes
(UI. Urbana - Champaign)
Luiz Antonio Barrera San Martin
(Unicamp)
Ivan Struchiner (USP)
Dirk Töben (UFSCar)

Scientific Committee

Claudio Gorodski
(USP)
Marcos M. Alexandrino
(USP)
Frédéric Barbaresco
(Thales)
Michel Nguiffo Boyom
(Montpellier)

Round-table with the Editorial Board of the São Paulo Journal of Mathematics



*To be confirmed



IME USP



GSI'19 Program

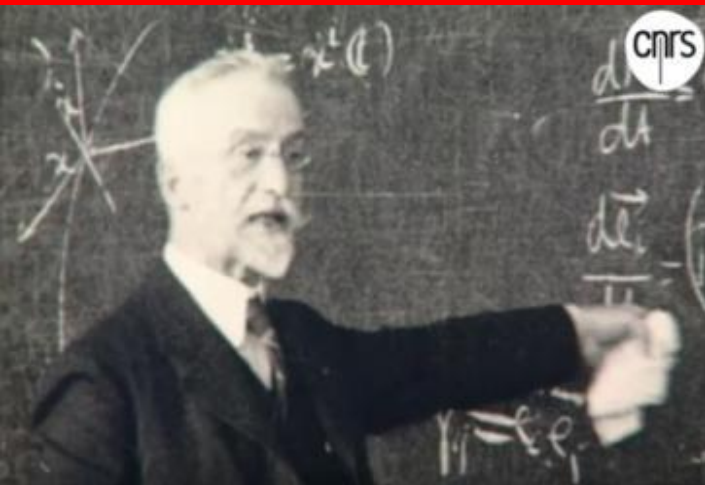
- More than **180** attendees from **21** different countries (France, Japan, Germany, USA, UK, Denmark, Brazil, Canada, Norway,...)
- **88** talks on 3 days (selection rate: **76%** based on **356 reviews**) and **16** posters
- **1 Invited Honorary Speaker**
 - Gérard LETAC (Université Paul Sabatier, Toulouse) – “Classifying the exponential families by moving a convex function”
- **1 Guest Honorary Speaker**
 - Karl Friston (Wellcome Trust Centre for Neuroimaging), “Markov Blankets and Bayesian Mechanics”
- **3 Keynote Speakers**
 - Elena Celledoni (Norwegian University of Science and Technology), “Structure preserving algorithms for geometric numerical integration”
 - Gabriel Peyré (CNRS, Ecole Normale Supérieure), “Optimal Transport for Machine Learning”
 - Jean-Baptiste Hiriart-Urruty (Université de Toulouse), “Pierre de FERMAT (ca. 1605-1665): lawyer, philologist and illustrious mathematician ... but enigmatic”



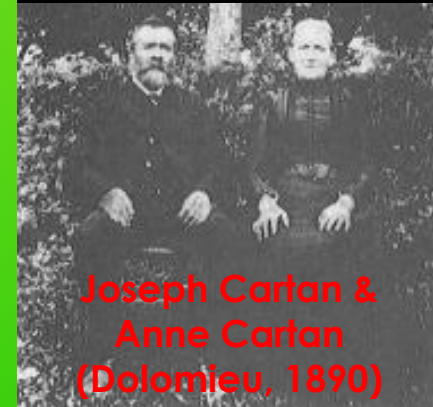
Elie Cartan 150th Birthday 1869-2019



150 years ago, April 9th 1869, was born a spirit, raised to the heat of the forge and the sound of the anvil and the hammer of his father Joseph, blacksmith of little Dolomieu village.



"des paysans sans prétention qui, au cours de leur longue vie, ont montré à leurs enfants un exemple de travail accompli avec joie et d'acceptation courageuse des fardeaux" - Elie Cartan

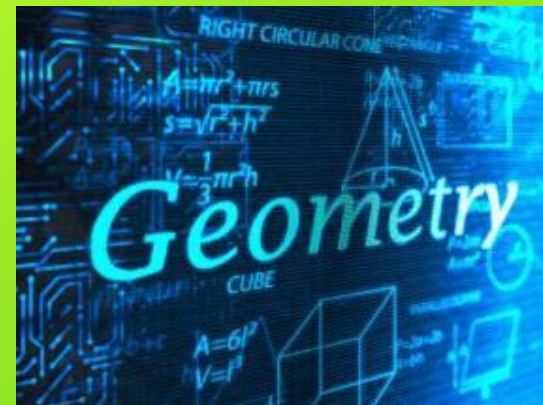


Henri Cartan Testimony on his father Elie Cartan:
<https://www.youtube.com/watch?v=GJ9NwEwUcyY>

GSI'19: 18 sessions



- Probability on Riemannian Manifolds
- Optimization on Manifold
- Shape Space
- Statistics on Non-linear Data
- Lie Group Machine Learning
- Statistical Manifold and Hessian Information Geometry
- Monotone Embedding and Affine Immersion of Probability Models
- Non-parametric Information Geometry
- Divergence Geometry
- Computational Information Geometry
- Wasserstein Information Geometry/Optimal Transport
- Geometric Structures in Thermodynamics and Statistical Physics
- Geometric and Structure-Preserving Discretizations
- Geometry of Quantum States
- Geometry of Tensor-Valued Data
- Geometric Mechanics
- Geometric Science of Information Libraries
- Poster Session





Guest Honorary speaker

G rard Letac

Classifying the exponential families by moving a convex function



G rard Letac Emeritus at the Universit  Paul Sabatier in mathematics. Birth in 1940. Undergraduate and graduate studies Universit  de Caen, Agr gation in math matiques in 1962. Doctorat d'Etat Clermont in 1972 (Thesis advisor Paul Malliavin). Professor at the Universit  Paul Sabatier from 1973 to 2003. Other positions as maitre- assistant in Orsay from 1962 to 1966; associated professor, University of Montr al from 1966 to 1969; chairman of the computer science department at IUT de Clermont from 1969 to 1973. Supervision of 26 doctorate thesis, and publications of 130 papers.

Scientific interests:

- Harmonic analysis and probabilities: Markov chains on permutations ('Libraries'); Gelfand pairs and group actions on Markov chains, homogeneous trees; Dirichlet processes.
- Random matrices: Random walks on $SL(2;R)$ and random continuous fractions. Wishart and non central Wishart laws on symmetric cones.
- Theoretical statistics: Fisher information; exponential families and their variance functions; Gaussian and discrete graphical models.



Invited Honorary speaker

Karl Friston

Markov blankets and Bayesian mechanics



Karl Friston (MB, BS, MA, MRCPsych, FMedSci, FRSB, FRS, Wellcome Principal Fellow, Scientific Director: Wellcome Trust Centre for Neuroimaging, Institute of Neurology, UCL). Karl Friston is a theoretical neuroscientist and authority on brain imaging. He invented statistical parametric mapping (SPM), voxel-based morphometry (VBM) and dynamic causal modelling (DCM). These contributions were motivated by schizophrenia research and theoretical studies of value-learning, formulated as the disconnection hypothesis of schizophrenia. Mathematical contributions include variational Laplacian procedures and generalized filtering for hierarchical Bayesian model inversion. Friston currently works on models of functional integration in the human brain and the principles that underlie neuronal interactions. His main contribution to theoretical neurobiology is a free-energy principle for action and perception (active inference). Friston received the first Young Investigators Award in Human Brain Mapping (1996) and was elected a Fellow of the Academy of Medical Sciences (1999). In 2000 he was President of the international Organization of Human Brain Mapping. In 2003 he was awarded the Minerva Golden Brain Award and was elected a Fellow of the Royal Society in 2006. In 2008 he received a Medal, College de France and an Honorary Doctorate from the University of York in 2011. He became of Fellow of the Royal Society of Biology in 2012, received the Weldon Memorial prize and Medal in 2013 for contributions to mathematical biology and was elected as a member of EMBO (excellence in the life sciences) in 2014 and the Academia Europaea in (2015). He was the 2016 recipient of the Charles Branch Award for unparalleled breakthroughs in Brain Research and the Glass Brain Award, a lifetime achievement award in the field of human brain mapping. He holds Honorary Doctorates from the University of Zurich and Radboud University.



Keynote speaker Elena Celledoni

Structure preserving algorithms for geometric numerical integration



Elena Celledoni (Professor at Department of Mathematical Sciences, Norwegian University of Science and Technology (NTNU), Trondheim, Norway). Elena Celledoni received her Master degree in mathematics from the University of Trieste in 1993, and her Ph.D in computational mathematics from the University of Padua, Italy, 1997. She held post doc positions at the University of Cambridge, UK, at the Mathematical Sciences Research Institute, Berkeley, California and at NTNU. Her research field is in numerical analysis and in particular structure preserving algorithms for differential equations and geometric numerical integration.



Keynote speaker Gabriel Peyré

Optimal Transport for Machine Learning



Gabriel Peyré (CNRS and Ecole Normale Supérieure).

Gabriel Peyré is senior researcher at the Centre Nationale de Recherche Scientifique (CNRS) and professor at the Ecole Normale Supérieure, Paris. His research is focused on developing mathematical and numerical tools for imaging sciences and machine learning. He is the creator of the "Numerical tour of data sciences" (www.numerical-tours.com), a popular online repository of Python/Matlab/Julia/R resources to teach mathematical data sciences. His research was supported by a ERC starting grant (SIGMA-Vision, 2010-2015) and is now supported by a ERC consolidator grant (NORIA 2017-2021). He is the 2017 recipient of the Blaise-Pascal prize from the French Academy of sciences, awarded each year to a young applied mathematician.o.



Keynote speaker Jean-Baptiste Hiriart-Urruty

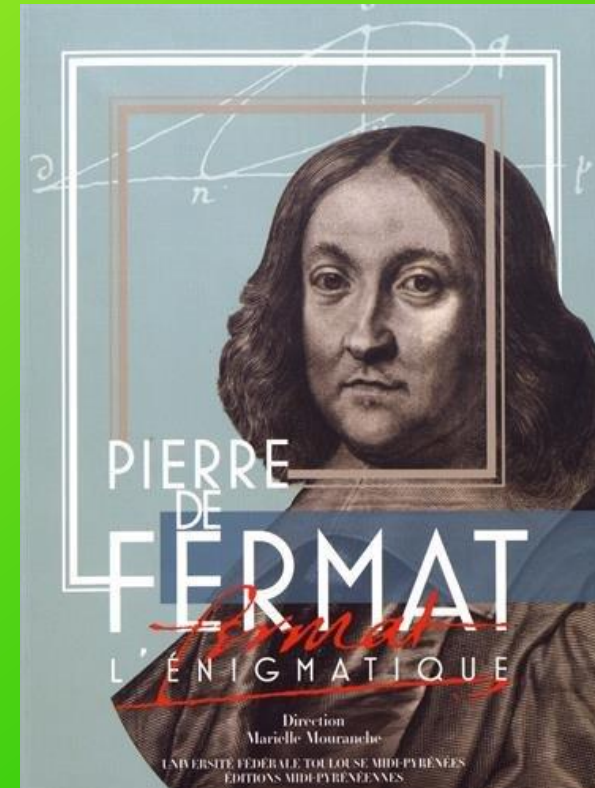
**Pierre de FERMAT (ca. 1605-1665):
lawyer, philologist and illustrious
mathematician ... but enigmatic**



Jean-Baptiste Hiriart-Urruty

(Toulouse University)

Jean-Baptiste Hiriart-Urruty is professor emeritus at the Université Paul Sabatier in Toulouse since 2015. He holds a PhD in mathematics from the Université Blaise Pascal in Clermon-Ferrand and an habilitation. He was full time professor in mathematics at University Paul Sabatier from 1981 to 2015. His research topics are variational calculus (convex, non smooth and applications) and optimization (global optimization, non smooth, non convex). He has also many contributions in the history of mathematics and mathematicians and in dissemination of mathematical science towards general public..





Thanks to ENAC administration & Local Organizing Team



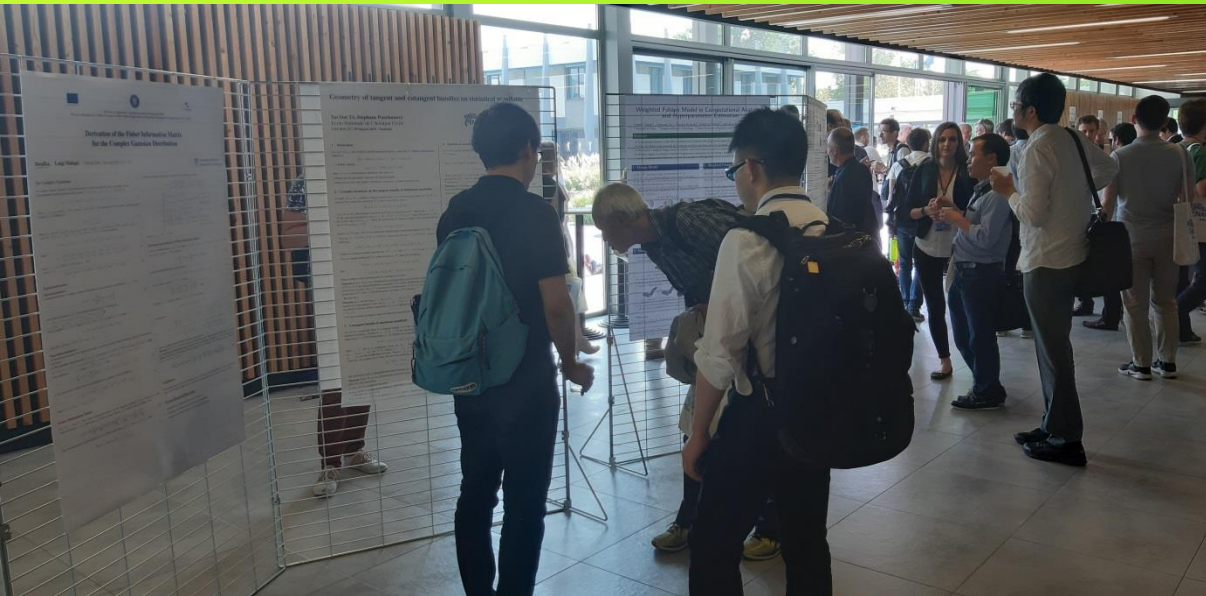


Thanks to 180 GSI'19 Attendees





Thanks to GSI'19 Attendees (Posters)





Thanks ENAC for cocktail with Wine Master & Cheese Master of G7 & GSI'19





Thanks to ENAC for Gala Diner





Last Publications on Geometric Science of Information

entropy

Differential Geometrical Theory of Statistics

Edited by
Frédéric Barbaresco and Frank Nielsen
Printed Edition of the Special Issue Published in Entropy

www.mdpi.com/journal/entropy



Volume 1, No. 1

Information, Entropy and Their Geometric Structures

Edited by
Frédéric Barbaresco and
Ali Mohammad-Djafari

Printed Edition of the Special Issue Published in Entropy

www.mdpi.com/journal/entropy



Journal of Communication Technology

entropy

Joseph Fourier 250th Birthday Modern Fourier Analysis and Fourier Heat Equation in Information Sciences for the XXIst Century

Edited by
Frédéric Barbaresco and Jean-Pierre Gazeau
Printed Edition of the Special Issue Published in Entropy

www.mdpi.com/journal/entropy



Information Geometry

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Harsh Manohar (Tokyo)

Springer

Frank Nielsen
Frank Critchley
Christopher T. J. Dodson Editors

Computational Information Geometry

For Image and Signal Processing

Springer

Jean-Louis Koszul
Yi Ming Zou

Introduction to Symplectic Geometry

Science Press
Beijing

Springer



GSI'21 in ...

Paris

Candidates of local host:

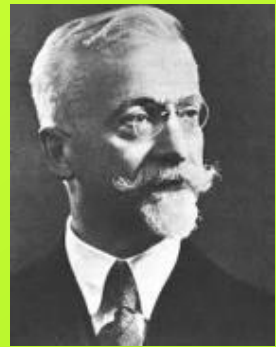
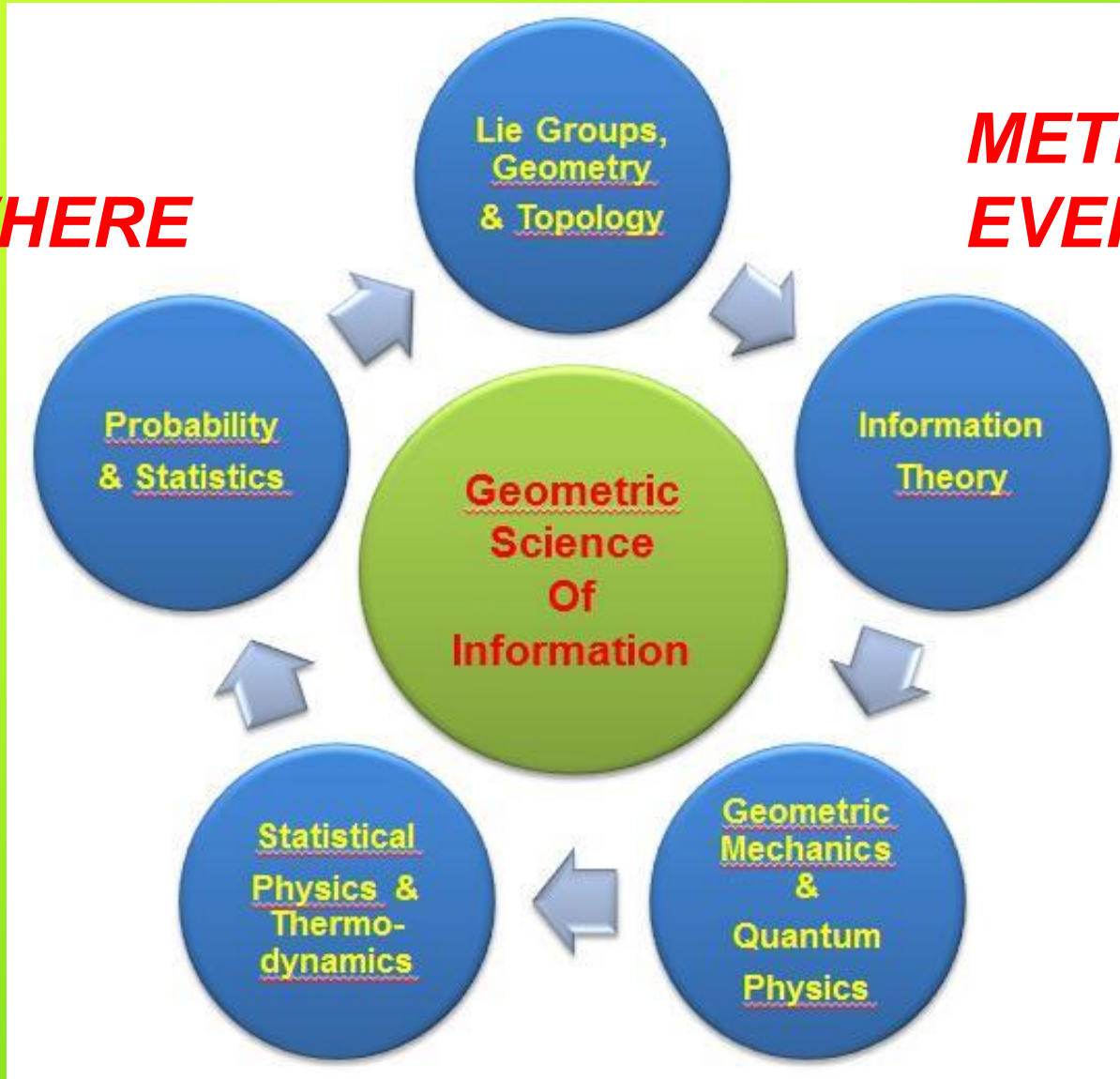
- IPP (Institut Polytechnique de Paris)
- Mine ParisTech
- Sorbonne University (SCAI lab)
- Institut Henri Poincaré
- ... ?



A new Grammar of Information

**GROUP
EVERYWHERE**

**METRIC
EVERYWHERE**



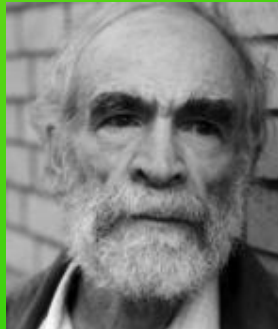
Elie Cartan



Maurice Fréchet



Henri Poincaré



Misha Gromov

“Mathematics is the art of giving the same name to different things” – Henri Poincaré



Elie Cartan: Group Everywhere (Henri Poincaré review of Cartan's Works)

RAPPORT SUR LES TRAVAUX DE M. CARTAN

fait à la Faculté des Sciences de l'Université de Paris.

PAR

H. POINCARÉ.



Si alors on dépouille la théorie mathématique de ce qui n'y apparaît que comme un accident, c'est-à-dire de sa matière, il ne restera que l'essentiel, c'est-à-dire la forme; et cette forme, qui constitue pour ainsi dire le squelette solide de la théorie, ce sera la structure du groupe.

M. CARTAN a fait faire des progrès importants à nos connaissances sur trois de ces catégories, la 1^{ère} la 3^e et la 4^e. Il s'est principalement placé au point de vue le plus abstrait de la structure, de la forme pure, indépendamment de la matière, c'est-à-dire, dans l'espèce, du nombre et du choix des variables indépendantes.

Conclusions.

On voit que les problèmes traités par M. CARTAN sont parmi les plus importants, les plus abstraits et les plus généraux dont s'occupent les Mathématiciens; ainsi que nous l'avons dit, la théorie des groupes est, pour ainsi dire, la Mathématique entière, dépouillée de sa matière et réduite à une forme pure. Cet extrême degré d'abstraction a sans doute rendu mon exposé un peu aride; pour faire apprécier chacun des résultats, il m'aurait fallu pour ainsi dire lui restituer la matière dont il avait été dépouillé; mais cette restitution peut se faire de mille façons différentes; et c'est cette forme unique que l'on retrouve ainsi sous une foule de vêtements divers, qui constitue le lien commun entre des théories mathématiques qu'on s'étonne souvent de trouver si voisines.



“the problems addressed by Elie Cartan are among the most important, most abstract and most general dealing with mathematics; group theory is, so to speak, the whole mathematics, stripped of its material and reduced to pure form. This extreme level of abstraction has probably made my presentation a little dry; to assess each of the results, I would have had virtually render him the material which he had been stripped; but this refund can be made in a thousand different ways; and this is the only form that can be found as well as a host of various garments, which is the common link between mathematical theories that are often surprised to find so near”

H. Poincaré





Maurice Fréchet: Metric Everywhere

LES ESPACES ABSTRAITS TOPOLOGIQUEMENT AFFINES.

PAR

MAURICE FRÉCHET

à STRASBOURG.

Un grand nombre des propriétés topologiques de l'espace euclidien s'étendent immédiatement à tous les espaces où une définition de la limite étant donnée (qui est en général imposée par la nature des éléments ou points de l'espace et les applications qu'on a en vue), cette définition peut s'exprimer par l'intermédiaire d'une *distance*.¹ Nous entendons par là qu'à tout couple A, B d'éléments ou points de l'espace considéré correspond un nombre $(A, B) = (B, A) \geq 0$, qui n'est nul que si A et B ne sont pas distincts et qui satisfait aux deux conditions suivantes:

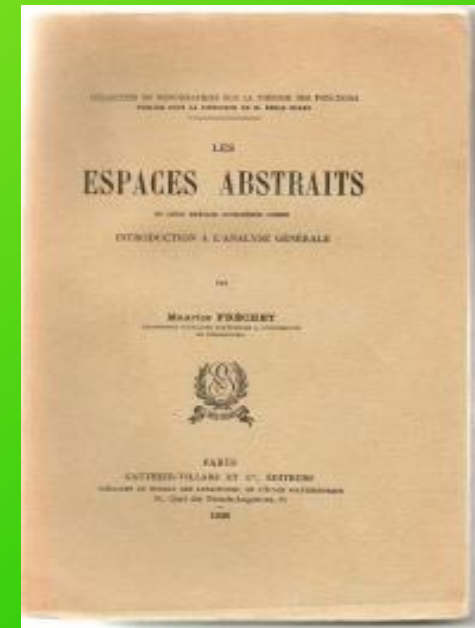
I. Pour trois points A, B, C arbitraires, on a toujours

$$(A, B) \leq (A, C) + (C, B).$$

II. La condition nécessaire et suffisante pour qu'une suite de points A_1, A_2, \dots de cet espace tende vers le point A de cet espace est que la distance (A, A_n) tende vers zéro.

Un tel espace sera appelé un espace (D) (initiale de distance).¹ Dans le cas où l'on n'impose pas la condition I, (A, B) sera un écart¹ et l'espace sera un espace (E)¹.

- Maurice Fréchet made major contributions to the **topology of point sets** and introduced the entire **concept of metric spaces**.
- His dissertation opened the entire field of **functionals on metric spaces** and introduced the notion of compactness.
- He has extended Probability in Metric space



1948 (Annales de l'IHP)

Les éléments aléatoires de nature quelconque
dans un espace distancié

Extension of Probability/Statistic in abstract/Metric space